

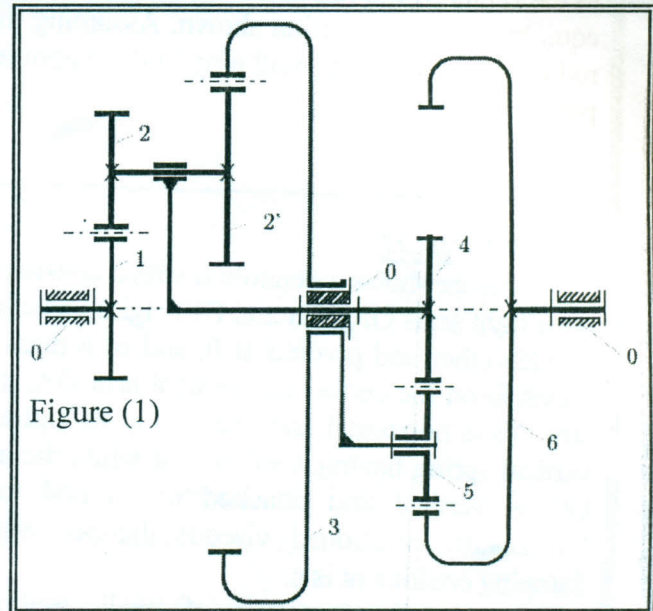
## THEORY OF MACHINES

### Question 1:

The sun gear 1, of the planetary gear train, has 26 external gear teeth, the planet gear 2 has 22 external gear teeth, the planet gear 2' has 30 external gear teeth, the sun gear 4 has 20 external gear teeth, the planet gear 5 has 18 external gear teeth, and the ring gears 3, 6 are internally teathed.

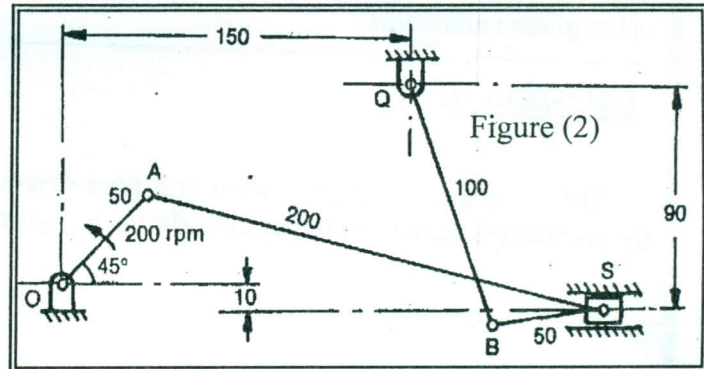
The gears 2 and 2' are fixed on the same shaft. The gear 1 rotates with input angular speed 100 rpm, in clockwise (CW) direction, and the ring gear 3 is fixed (not rotate). All the gears have the same module. **Find:**

- The number of teeth of ring gears 3, 6.
- The angular velocity and direction of rotation (CW or CCW) of each gear.



### Question 1:

Figure (2) shows a mechanism in which O and Q are the fixed centres. Determine the velocity and acceleration of the slider S, and the angular velocity and angular acceleration of the link BQ for the given configuration.

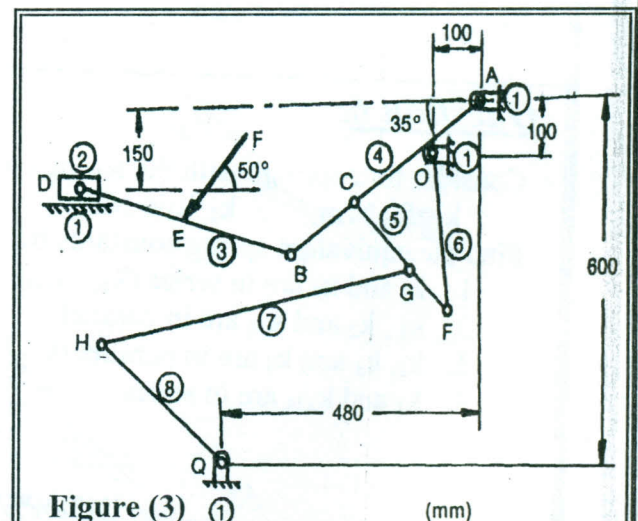


### Question 3:

Figure (3) shows a schematic diagram of an eight-link mechanism. The link lengths are ;

$AB = 450$	$OF = FC = 250$
$AC = 300$	$CG = 150$
$BD = 400$	$HG = 600$
$BE = 200$	$QH = 300$

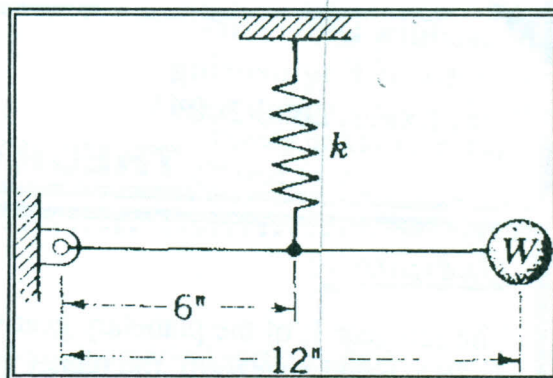
Determine the required shaft torque on link 8 for static equilibrium against an applied load of 400 N on the link 3





### Question 4:

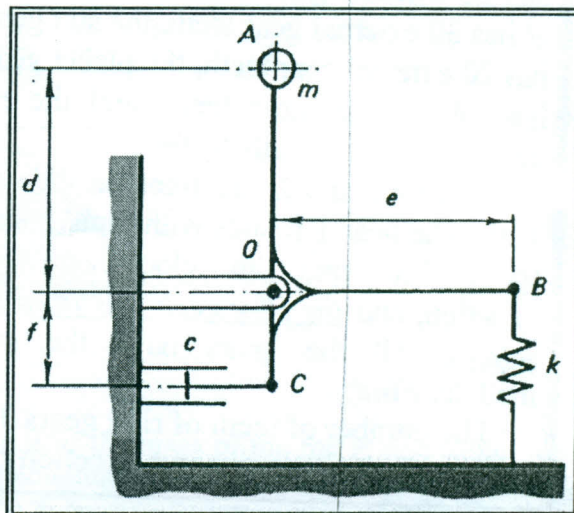
The figure shows a weight  $W = 15 \text{ lb}$  connected to a pivoted rod which is assumed to be weightless and very rigid. A spring having  $k = 60 \text{ lb/in}$  is connected to the center of the rod and holds the system in static equilibrium at the position shown. Assuming that the rod can vibrate with a small amplitude, determine the period of the motion.



### Question 5:

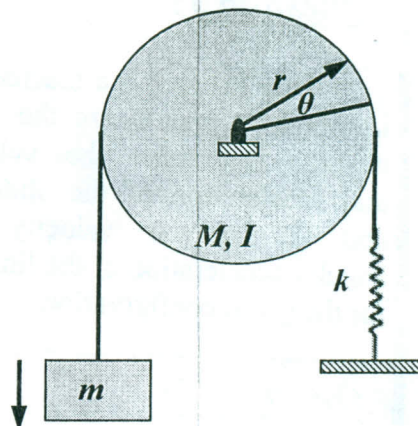
The figure shows a pendulum which consists of three light arms OA, OB and OC, rigidly attached to each other and pivoted at O, and of a mass  $m$  which is on the end of the vertical arm OA. The arm OB is horizontal and attached at its end to a vertical spring having a stiffness  $k$  while the arm OC is vertical and attached at its end to a horizontally positioned viscous damper whose damping coefficient is  $c$ .

Determine the frequency of small amplitude undamped oscillations of the pendulum about O and find the critical damping coefficient in terms of the given parameters.



### Question 6:

Drive the equations of motion and then determine the angular frequency for the system shown in figure



### Question 6:

Consider four springs with the spring constants :

$$k_1=50 \text{ N/m}, \quad k_2=100 \text{ N/m}, \quad k_3=200 \text{ N/m}, \quad k_4=300 \text{ N/m}.$$

Find the equivalent spring constants for the following combinations :

1.  $k_3$  and  $k_4$  are in series ( $k_{eq} = k_{34}$ )
2.  $k_1$ ,  $k_2$  and  $k_{34}$  are in parallel
3.  $k_2$ ,  $k_3$  and  $k_4$  are in parallel ( $k_{eq} = k_{234}$ )
4.  $k_1$  and  $k_{234}$  are in series

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